I've got all my life to live, I've got all my love to give, I will derive!	
Period	

- Analysis Calculus Quiz 18/19 No Calculators!
- 1. Iron Hans decided to keep track of his velocity as he biked the second leg of his triathlon. He later realized it could be modeled by the function $f(x) = \frac{-2^x}{3} + 18$ where f(x) is measured in miles per hour and x is measured in hours.
- a) What was the average rate of change of his velocity over the time interval x: [0, 4]? Include units
- b) Hans used his calculator to approximate f'(2) = -0.924. Use words to explain what this number means in the context of the problem. Include units in your explanation.

- c) Why can we be sure that the Intermediate value theorem applies to f(x) over x: [0, 4]?
- d) State one thing that the Intermediate Value Theorem would guarantee for this situation.
- 2. In the space on the right, sketch a graph of a function with x values A, B, C, and D (in that order) that satisfies the following conditions. Label the points of course!!
- i) The derivative at x=A is zero.
- ii) The derivative at x=B is a very large and positive number.
- iii) The function has a limit at x=C but no output.
- iv) The function has an output but no limit at x=D.

3. The sewer pipes in my front yard exploded last week! The utility company started working on the pipe at 1:00, but had workers coming in and out over the next few hours (I know because I kept track).
Below are the number of workers on the project at 20 minute intervals after 1:00.

minutes after 1:00 (t)	0	20	40	60	80
Workers (y)	1	4	6	5	2

a) Approximate the derivative at t=60 minutes. Include units.

b) Use the trap rule to estimate the definite integral over the 80-minute period as accurately as possible and state units.

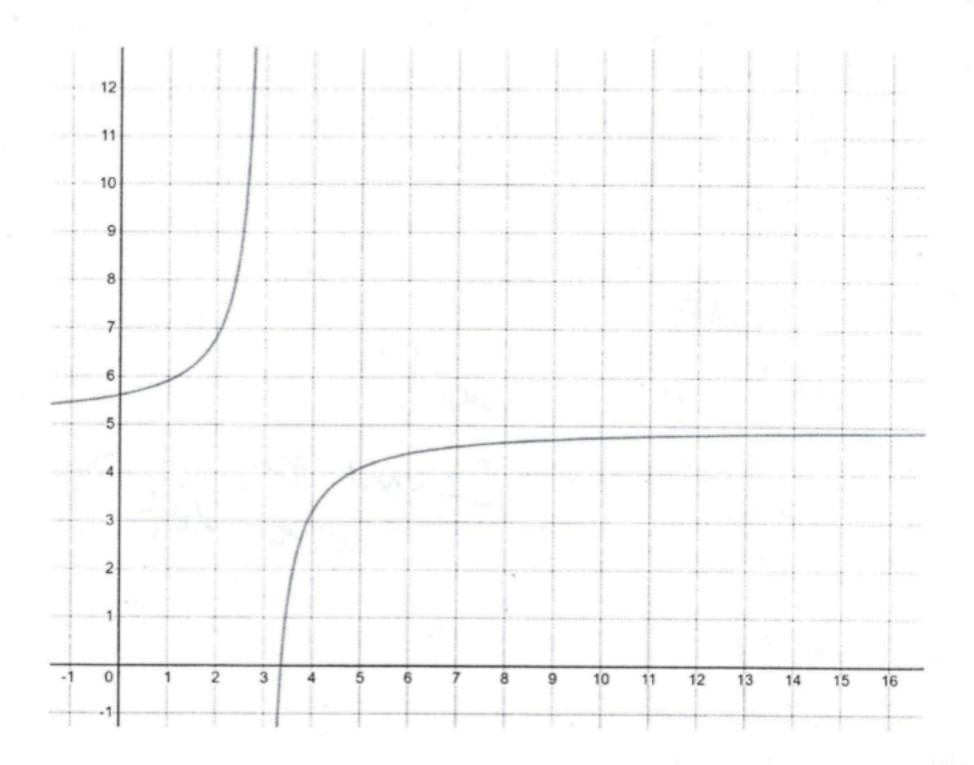
4. Evaluate the following limits or state that they do not exist. Show algebraic work for full credit.

a)
$$\lim_{x\to 3} \frac{\frac{1}{x^2} - \frac{1}{9}}{x-3}$$

b)
$$\lim_{x\to 3} \frac{\frac{1}{x^2} + \frac{1}{9}}{x-3}$$

5. The following equation implies a certain function and important information about that function. Use your calculus knowledge to interpret the equation's hidden information. To demonstrate your understanding, draw an accurate picture of a function, a tangent line to the function, and a specific point of tangency.

$$\lim_{x \to e} \frac{\ln x - 1}{x - e} = \frac{1}{e}$$



6. The graph above shows f(x).

a) Using the graph as reference, fill in the blanks (with numerical values, not variables). Show your work on the graph so that I can follow your reasoning.

The limit of f(x) as x approaches infinity seems to be _____ because if x >____ then f(x) will be within 0.5 units of its limit.

The limit of f(x) as x approaches _____ from the left side seems to be positive infinity because if x is within ____ units of _____ from the left side then f(x) > 10

b) In the space below, sketch a graph of f'(x).

7. Use the formal definition of the derivative of a function to prove:

$$\frac{d}{dx}\sqrt{x} = \frac{1}{2\sqrt{x}}$$

(hint: conjugate!)

- 8. Given $f(x) = 2x^3 4x + 5$
 - a) Use the power rule to find f'(x).

b) Find all points on f(x) where the instantaneous rate of change is 21.