

No Calculators! Because you don't have a calculator you don't need to simplify any answers.

1. You are dealt 5 cards from a deck of 52. The first two cards are an Ace and a King. What is the probability that you will complete the A-K-Q-J-10 straight (suits do not matter)?

$$\frac{1 \binom{4}{1}^3}{\binom{50}{3}}$$

$$\frac{\binom{4}{1}^3}{\binom{50}{3}}$$

2. In Europe, 90% of all households have a television. 50% of all households have a television and DVD player. 1% of all households own a DVD player, but not a television.

- a) What is the probability that a household has a DVD player, given that it has a television?

	TELEVISION	
DVD	50%	1%
NO DVD	40%	9%

$$\frac{5}{9}$$

- b) Are the events owning a television and owning a DVD player independent events or not? Show your work to support your answer.

No

$$P(\text{DVD}) = 51\%$$

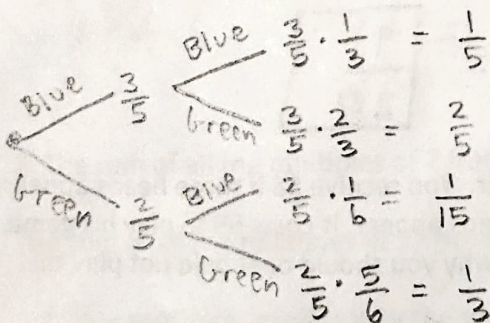
Since $P(\text{DVD}) \neq P(\text{DVD}|\text{TV})$

$$P(\text{DVD}|\text{TV}) = \frac{5}{9} \approx 55\%$$

the answer is no

3. Jar A has 3 blue and 2 green marbles, and Jar B has 1 blue and 4 green marbles. A random marble is drawn from Jar A and placed in Jar B. Then a random marble is drawn from Jar B. [6]

- a) Draw a tree diagram of the given information.



- b) $P(\text{the second marble is green}) =$

$$\frac{2}{5} + \frac{1}{3} = \frac{11}{15}$$

- c) $P(2^{\text{nd}} \text{ marble is green} | 1^{\text{st}} \text{ marble was blue}) =$

$$\frac{2}{5} / \frac{3}{5} = \frac{2}{3}$$

- d) $P(1^{\text{st}} \text{ marble is blue} | 2^{\text{nd}} \text{ marble was green}) =$

$$\frac{2}{5} / \left(\frac{2}{5} + \frac{1}{3} \right) = \frac{6}{15} / \frac{11}{15} = \frac{6}{11}$$

4. A factory produces components of which 1% are defective. The components are packed in boxes of 10. A box is selected at random.

- a) Find the probability that the box contains exactly one defective component.

$$\left[\binom{10}{1} (0.01)^1 (0.99)^9 \right]$$

- b) Find the probability that there are at least 2 defective components in the box.

$$\left[1 - \binom{10}{1} (0.01)^1 (0.99)^9 - \binom{10}{0} (0.99)^{10} \right]$$

5. Three horses, A, B, and C, compete in four races. Assuming that each horse has equal chance of winning in each race,

- a) what is the probability that A wins two races and B and C win one race each?

$$\begin{array}{r} 36 \\ 81 \\ \hline 24 \\ 81 \\ \hline 3 \\ 81 \end{array}$$

$$\begin{array}{l} \text{--- } 2, 1, 1 \\ \text{--- } 3, 1, 0 \\ \text{--- } 4, 0, 0 \end{array}$$

$$2, 2, 0 \text{ --- } \frac{18}{81}$$

$$\frac{12}{81} = \boxed{\frac{4}{27}}$$

- b) what is the probability that the same horse wins all four races?

$$3 \cdot \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} \cdot \frac{1}{3} = \boxed{\frac{1}{27}}$$

6. Big Al has a game where he tosses three fair coins in the air. You receive \$8 if three heads appear, \$4 if two heads appear, \$2 if one head appears, and \$1 if no heads appear. It costs \$5 to play his game. What is the expected value of playing this game? Explain why you should or should not play this game?

$$8 \cdot \frac{1}{8} + 4 \cdot \frac{3}{8} + 2 \cdot \frac{3}{8} + 1 \cdot \frac{1}{8} = 1 + \frac{3}{2} + \frac{3}{4} + \frac{1}{8}$$

$$= \frac{8+12+6+1}{8} = \frac{27}{8}$$

$$\frac{27}{8} - 5 = -\frac{13}{8}$$

$$\boxed{-\$ \frac{13}{8}}$$

We should not play this game. Since, the expected value is negative, we cannot expect to profit instead, we would be losing money.