

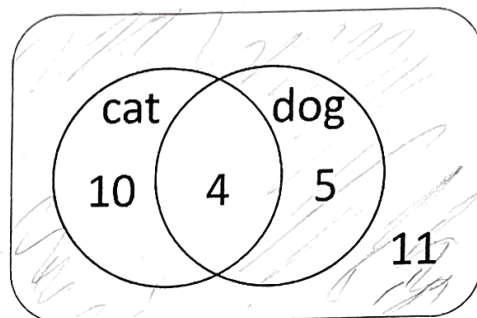
**For Questions 1 and 2:** The Venn Diagram on the right shows the result of a survey, "do you own a cat or a dog?"  
Let  $C$  = cat and  $D$  = dog.

1. Which of the following represents  $11/30$  of the people surveyed?

(IMPORTANT: Circle ALL that apply)

a)  $P(C \cup D)$  (b)  $P(C' \cap D')$  c)  $P(C' \cap D')$

d)  $P(C \cap D)'$  (e)  $P(C \cup D)'$



2. What is  $P(D|C')$ ?

D given not C

$$P = \frac{5}{16}$$

3. Two fair, 6-sided dice are rolled (each one numbered 1-6). Find...

a)  $P(\text{sum is } 10) = \frac{1}{12}$

$$\begin{array}{cc} 4 & 6 \\ 5 & 5 \\ 6 & 4 \end{array}$$

b)  $P(\text{"sum is greater than 7" OR "sum is an odd number"}) = \frac{27}{36}$

$$\begin{array}{cccc} 2 & 6 & 6 & 2 \\ 3 & 5 & 5 & 3 \end{array} = \frac{5}{36}$$

$$\begin{array}{cc} 3 & 6 \\ 6 & 3 \end{array} = \frac{4}{36}$$

$$\begin{array}{cc} 4 & 6 \\ 6 & 4 \end{array} = \frac{3}{36}$$

$$\begin{array}{cc} 5 & 6 \\ 6 & 5 \end{array} = \frac{2}{36}$$

c)  $P(\text{"sum is greater than 7" | "sum is an odd number"}) = \frac{6}{18}$

d) The 2 dice are rolled 10 times in a row and the sum of the dice is recorded each time. What is the probability that the sum was more than 10, exactly 4 times?

$$P = \frac{1}{18}$$

$$n = 10$$

$$k = 4$$

$$\binom{10}{4} \left(\frac{1}{12}\right)^4 \left(\frac{11}{12}\right)^6$$

4. Krafty Callie has a strange deck of cards with 6 Aces, 6 Kings, 6 Queens, and 6 Jacks. Using this deck, suppose you draw a card, DON'T replace it, and then draw another card. Find...

a)  $P(\text{drawing an Ace on the 2nd card, given that your 1st card was an Ace}) =$

$$\frac{5}{23}$$

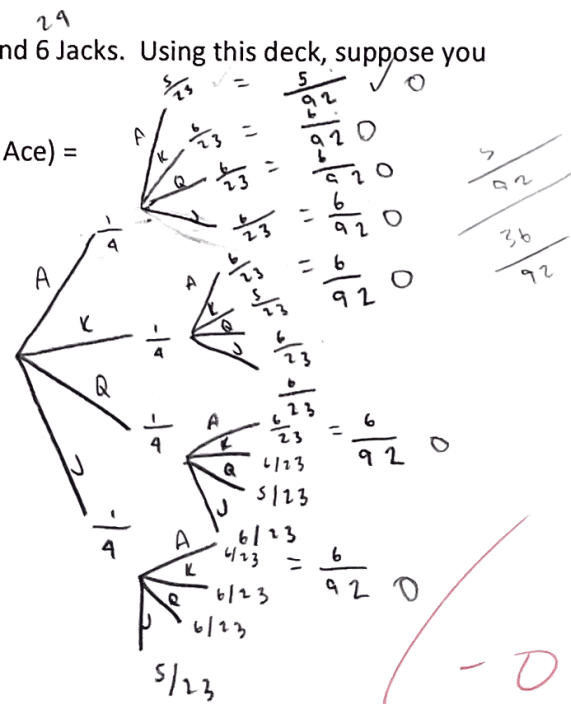
b)  $P(\text{drawing 2 Aces}) =$

$$\frac{23}{92}$$

$$\frac{5}{92}$$

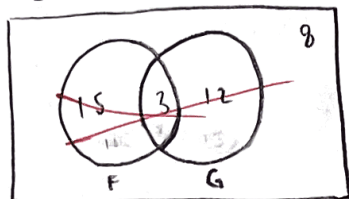
c)  $P(\text{drawing 2 Aces, given that at least one of the cards is an Ace}) =$

$$\frac{5}{41}$$

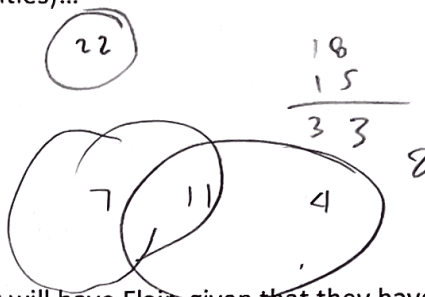


5. In a certain Analysis H class of 30 students, 18 of them have Flair, and 15 of them have Gumption. If 8 of them have neither Flair nor Gumption (don't worry, they have other great qualities)...

a) Draw a Venn Diagram for this premise.



(-1)



b) What is the probability that a randomly selected student will have Flair, given that they have Gumption?

$$P = \frac{3}{15} \quad (-1)$$

$$\frac{11}{15}$$

c) Are the events "have Flair" and "have Gumption" mutually exclusive? Give a short (one sentence) explanation to justify your answer.

NO, because both can happen at the same time.

6. In a normal 52-card deck there are 12 face cards and 40 non-face cards. Felix draws a random card from the deck.

- If the card is a face card, Felix rolls a 6-sided die and records the number (1-6)

- If the card is a non-face card, Felix rolls a 10-sided die and records the number (1-10)

a)  $P(\text{choosing a face card and then rolling an odd number}) =$

$$\frac{12}{52} \cdot \frac{1}{2} = \frac{12}{104} \quad \checkmark$$

b)  $P(\text{he records an 8} \mid \text{he chose a non-face card}) =$

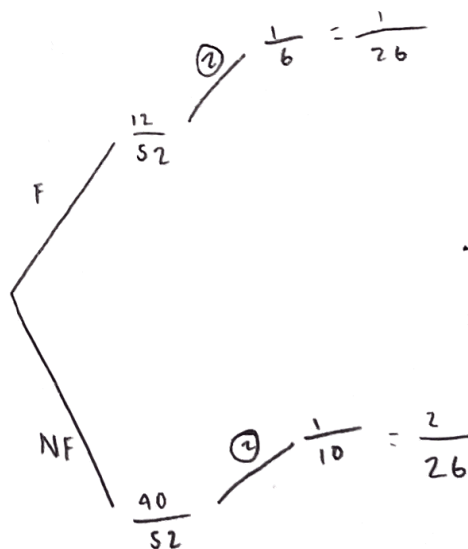
$$\frac{1}{10} \quad \checkmark$$

c)  $P(\text{he chose a non-face card} \mid \text{he records an 8}) =$

1

d)  $P(\text{he chose a face card} \mid \text{he records a 2}) =$

$$\frac{1}{3}$$



$$\frac{4}{52} = \frac{2}{26}$$

-2