Analysis H – Hahn / Hlasek / Tantod
MT Exam 2: Polar, 3D, parametric, vectors
No Calculators

Midtermined student:	
	Period:

100 points

#### Part 1: Polar Graphing

Questions 1-4 are Multiple Choice. Circle the best answer. [2 pts each]

- 1. In the polar system, the graph of  $r=7\cos 8\theta$  is a
  - a) Rose curve with 8 petals
- b) Rose curve with 16 petals
  - c) Rose curve with 7 petals
- d) Lemniscate symmetric about the line  $\theta = 0$  e) None of the above
- 2. In the polar system, the graph of  $r^2 = 32 \sin 2\theta$  is a \_\_\_\_\_.
  - a) Rose curve with 2 petals
- b) Rose curve with 4 petals
- c) Rose curve with 32 petals
- d) Lemniscate symmetric about the line  $\theta=0$  e) None of the above
- 3. In the polar system, the graph of  $r = 4 8 \sin \theta$  is a \_\_\_\_\_.
  - a) Limacon with an inner loop b) Dimpled Limacon

c) Cardioid

- d) Convex Limacon
- e) None of the above
- 4. In the Polar System, the graphs of  $r^2 = 4 \sin 2\theta$  and  $r^2 = 4 \cos 2\theta$  have \_\_\_\_\_\_ points of intersection.
  - a) less than 3
- b) 3
- c) 4

d) 5

e) More than 5

Free Response: Show all your work to receive full credit.

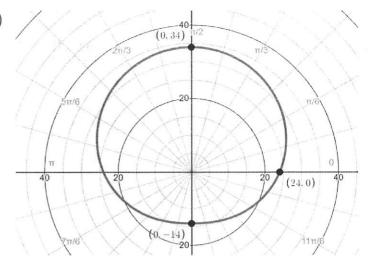
5. Convert the polar equation to rectangular form. Write your answer as a function y in terms of x. [3 pts]

$$r = \frac{2}{1 - \sin \theta}$$

6. On the graphs below, the labeled points are all in rectangular form. Write a <u>polar</u> equation to match each graph. Write each answer as a function r in terms of theta. [3 pts each]

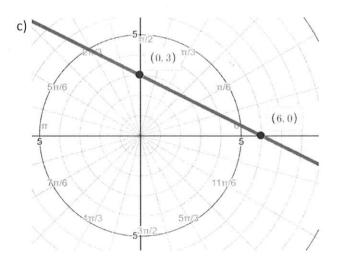
a) (-32.0) T (-20.0) (0.6) (0.6)

b)

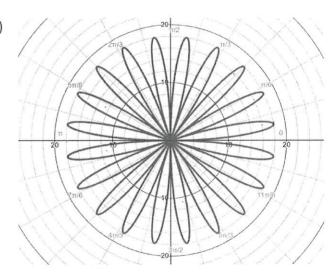


Equation:

Equation:



d)



Equation:

Equation:

7. Give the polar coordinates of the tip of the 1<sup>st</sup> petal in the graph of 6(d) above. (By the "1<sup>st</sup> petal", we mean the petal that is in the first quadrant, closest to the positive x-axis). [2 pts]

### Part 2: 3D Graphing

# Questions 1-4 are Multiple Choice. Circle the best answer. [2 pts each]

- 1. In the 3D system, the graph of  $y^2 \frac{x^2}{6} z = 0$  is a \_\_\_\_\_\_.
  - a) Parabolic Cylinder

b) Elliptic Cylinder

c) Hyperbolic Cylinder

- d) Hyperbolic Paraboloid
- e) Elliptic Paraboloid
- 2. In the 3D system, the graph of  $\frac{x^2}{3} + \frac{y^2}{4} = \frac{z^2}{5}$  is a \_\_\_\_\_\_.
  - a) Elliptic Cone

b) Elliptic Paraboloid

c) Hyperboloid of 1 sheet

- d) Hyperboloid of 2 sheets
- e) Hyperbolic Paraboloid
- 3. In the 3D system, the **intersection** of the graphs of  $y = x^2 + z^2$  and x = 10 is a \_\_\_\_\_\_.
  - a) Ellipse, but not a Circle
- b) Circle

c) Parabola

d) Hyperbola

- e) Plane
- 4. In the 3D system, the intersection of the graphs of  $x^2 + z^2 = 25$  and 2x + 3y + 4z = 12 is \_\_\_\_\_\_.
  - a) Ellipse, but not a Circle
- b) Circle

c) Parabola

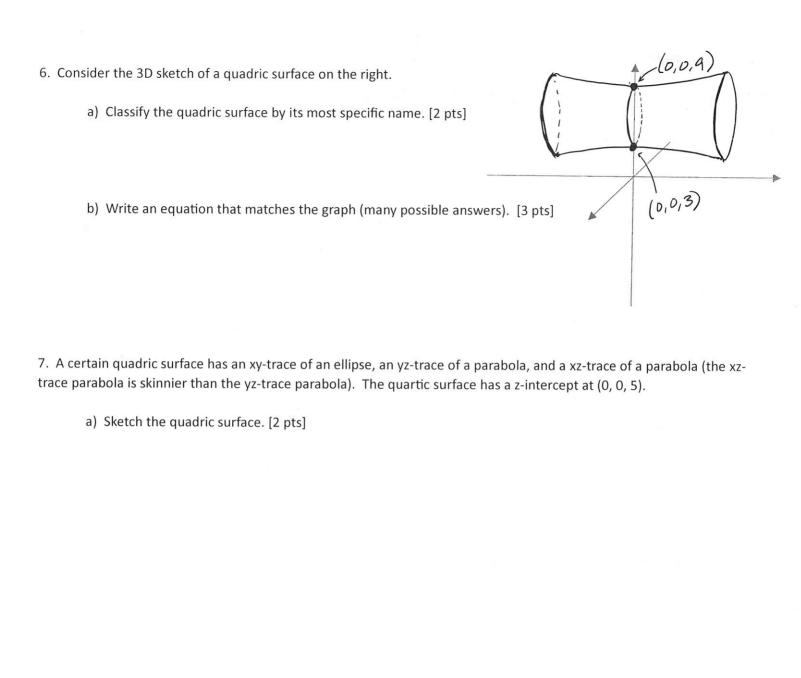
d) Hyperbola

e) Plane

Free Response: Show all your work to receive full credit.

- 5. Consider the graph of  $\frac{x^2}{9} + y^2 8y + z^2 = 25$  in the 3D system.
  - a) Classify the quadric surface by its most specific name [2 pts]

b) Find the y-intercept(s) of the graph. [3 pts]



b) Classify the quadric surface by its most specific name. [2 pts]

c) Write an equation that matches your graph (many possible answers). [3 pts]

# Part 3: Vectors and Parametric Equations

# Questions 1-4 are Multiple Choice. Circle the best answer. [3 pts each]

- 1. The graph of the set of parametric equations  $x(t) = 3 sin^2 t$  is a \_\_\_\_\_\_
  - a) circle
- b) ellipse
- c) parabola
- d) hyperbola
- e) spiral

- 2. Given: i, j, and k are standard unit vectors. Find |j k|.
- a) j b) -j c) <1, 0, -1> d)  $\sqrt{2}$
- 3. If  $\vec{u}$  goes from the door to the TV, and  $\vec{v}$  goes from the TV to the teacher's desk, which of the following directions BEST describes  $\vec{u} \times \vec{v}$  ?
  - a) from the ceiling to the floor
- b) from the floor to the ceiling
- c) from the TV to the door
- d) from the TV to the teacher's desk
- e) from the door to the teacher's desk
- 4. The equations of two lines are given below in parametric form. The two lines are \_\_\_\_\_\_

$$L_1 = \begin{cases} 2t - 4 \\ 5t + 3 \\ -7t - 2 \end{cases} \qquad L_2 = \begin{cases} -4t + 2 \\ -10t + 2 \\ 14t + 3 \end{cases}$$

- a) skew
- b) parallel
- c) intersecting but not perpendicular
- d) intersecting and perpendicular
- e) the same line

### Questions 5-8 are Multiple Choice. Circle the best answer.

- 5. If the area of triangle ABC = 10, and Angle A = Q, then  $|\overrightarrow{AB}| |\overrightarrow{AC}| \sin Q =$ 
  - a) 20
- b) 5
- c) 40
- d) 10
- e) not enough info

- 6. Find  $(k \times -j) \times j$ 
  - a) i

- b) -*i*
- c) k
- d) 0
- e) -k
- 7. In 2-D, consider  $\vec{u} = <-7.2>$  and  $\vec{v} = <5.1>$ . Which of the following most closely resembles  $proj_{\nu}\vec{u}$ ?
  - a)









8. If a ball is launched at a 15-degree angle of elevation at a velocity of 80 feet per second, which function most closely represents the height of the ball after t seconds?

a) 
$$h = -16t^2 + 80t$$

a) 
$$h = -16t^2 + 80t$$
 b)  $h = -\frac{1}{2}t^2 + 20t$  c)  $h = -16t^2 + 60t$ 

c) 
$$h = -16t^2 + 60t$$

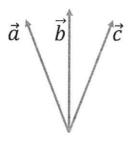
d) 
$$h = -\frac{1}{2}t^2 + 60t$$
 e)  $h = -16t^2 + 20t$ 

e) 
$$h = -16t^2 + 20t$$

#### Free Response

9. Find the rectangular equation of the plane through (3, 2, 4) that will be perpendicular to the pair of intersecting planes 3x + 2y - z = 6 and x - 2y - z = 4. [4 pts]

10. In the figure below, all three vectors are unit vectors. Draw the resultant vector of  $\vec{b} \times (\vec{c} \times \vec{a})$ . To receive full credit, your resultant vector must have a reasonably correct direction AND magnitude. [4 pts]



- 11. Consider the plane x 3y + 2z 13 = 0, with a line that is perpendicular to the plane. The line also passes through the point (-2, 1, -1).
  - a) Write the equation of the line in parametric form. [3 pts]

b) How far is the point (2, 4, 1) from the plane? Give your answer as a simplified fraction, and rationalize the denominator, if necessary. [3 pts]

12. Find the point where the line  $\langle x, y, z \rangle = \langle -1, 4, 0 \rangle + t \langle 2, 3, 1 \rangle$  intersects the plane x + 2y - 3z = 12. [4 pts]

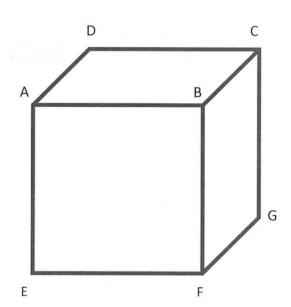
13.	Find two values of <i>m</i> that make the vectors	$<4,1,-7>$ and $< m,m^2,3>$ orthogonal. [4]	4 ntsl
	The tire raided of m that make the vectors	\ 1,1, / / and \ m, m , 5 / orthogonal.	T PLS

Questions 14 and 15 refer to the diagram on right, which shows cube with vertices labeled A-H (point H is the vertex that is behind the figure, out of sight).

14. Use the vertices to name a vector that has the same direction as the given cross product. Each of your answers should be a single vector, identified by 2 points. [1 pt each]

$$\overrightarrow{CA} \times \overrightarrow{CD}$$
\_\_\_\_\_

$$\overrightarrow{EA} \times \overrightarrow{EB}$$



15. Fill in the blank with a < , >, or = symbol to make the statement true. [1 pt]

$$|\overrightarrow{BA} \times \overrightarrow{BF}|$$
  $|\overrightarrow{EA} \times \overrightarrow{EB}|$